

# Understanding the dual-slope effect in crosstalk (EL-FEXT)

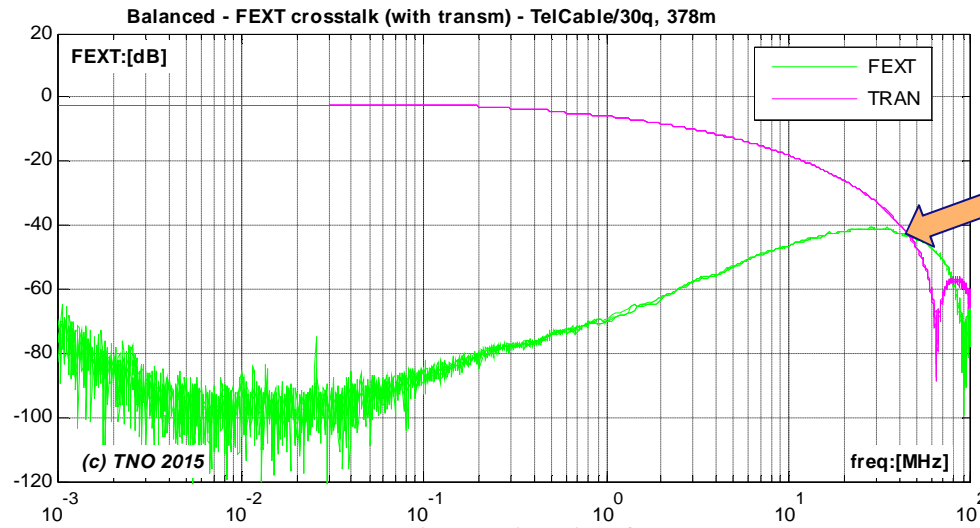
What causes this second order crosstalk effect in quad cables?

Rob F.M. van den Brink – TNO

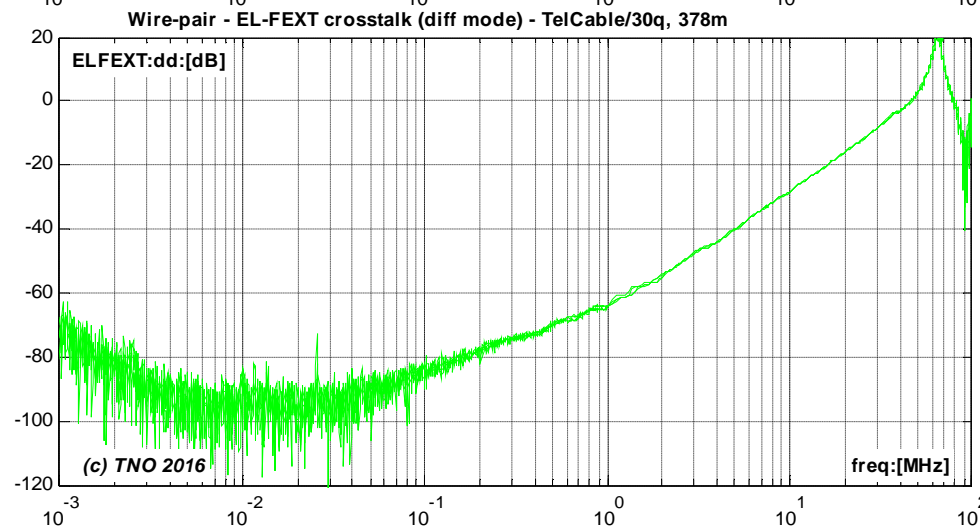
**TNO** innovation  
for life

# 1. FEXT crosstalk measurements in telephony cabling

An example: 30 quads, 378m, winded on a drum



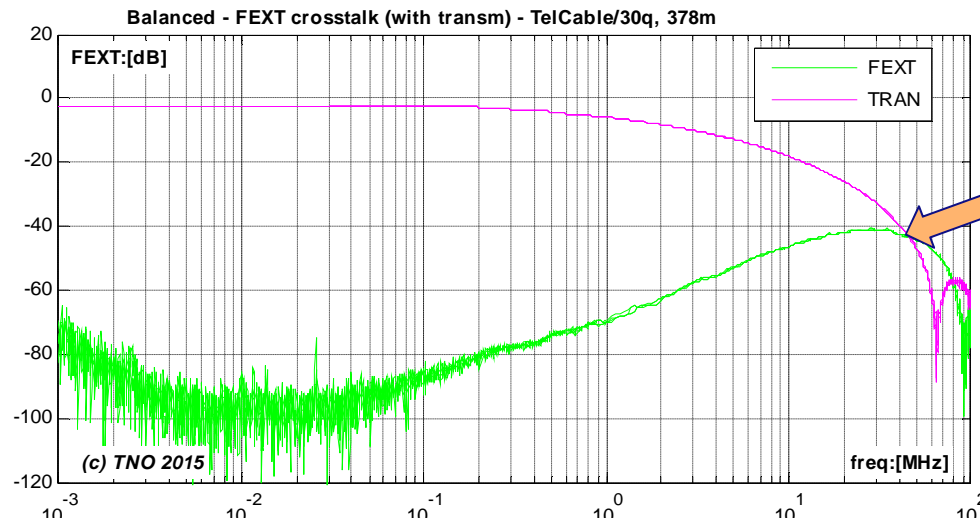
Crosstalk exceeds direct transmission



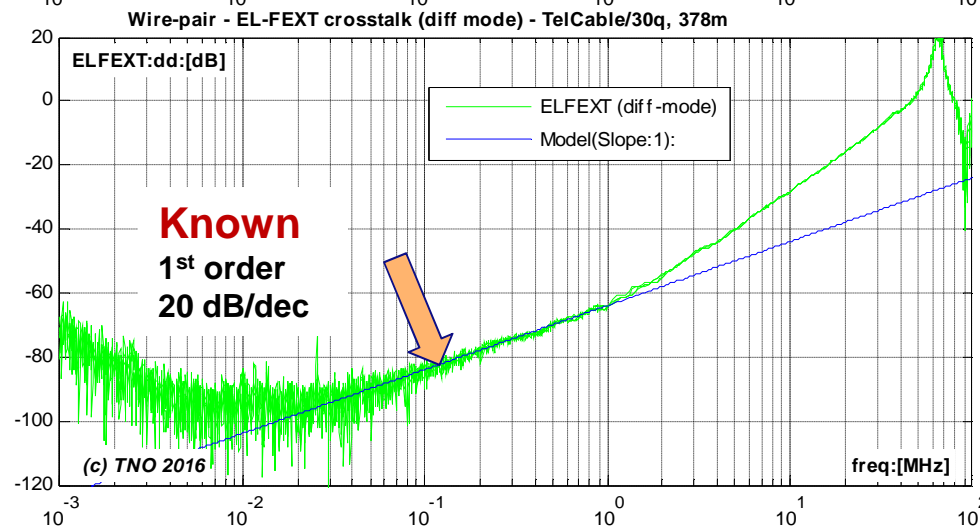
$$EL-FEXT = \frac{FEXT \text{ (crosstalk)}}{TRAN \text{ (signal)}}$$

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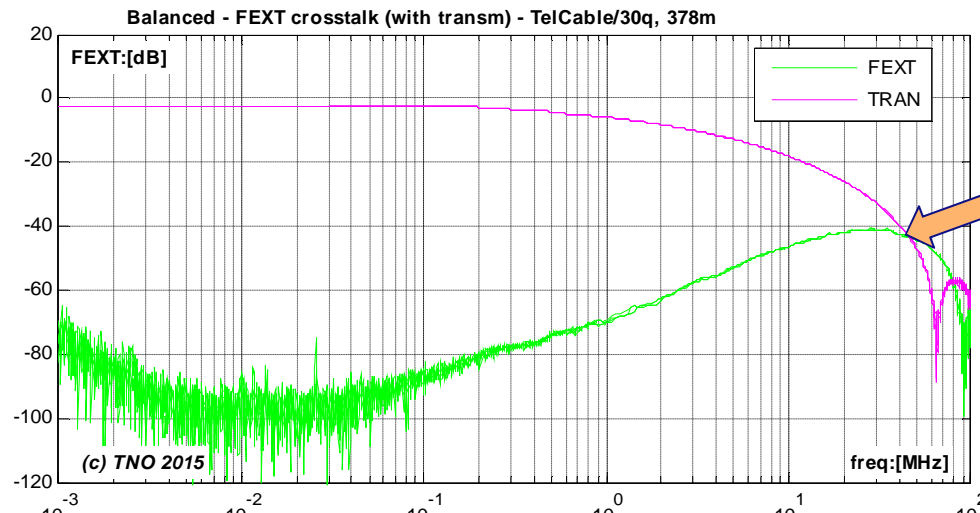
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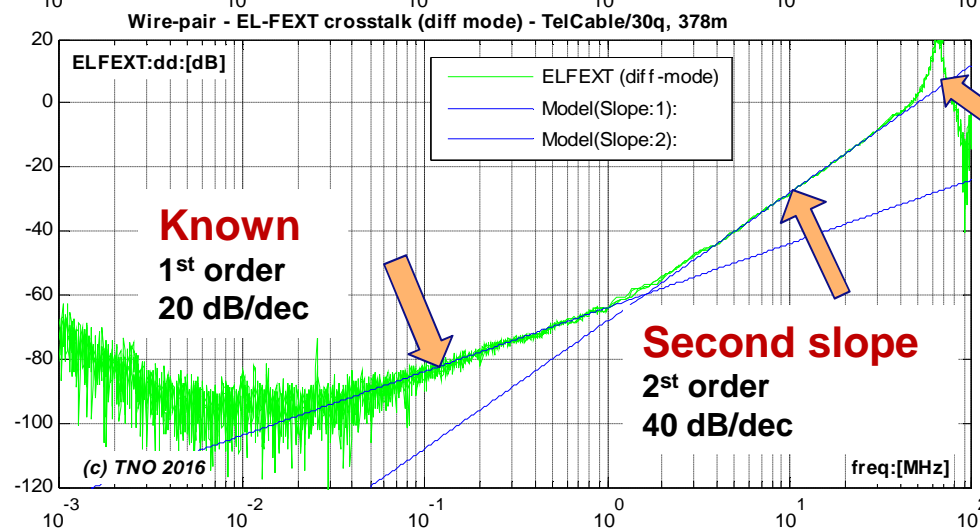
An example: 30 quads, 378m, winded on a drum



Crosstalk exceeds direct transmission



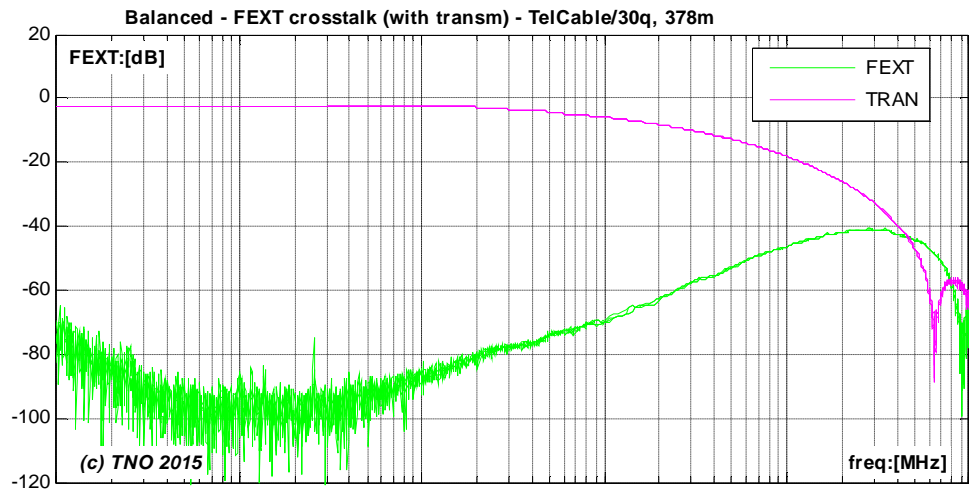
EL-FEXT > 0dB



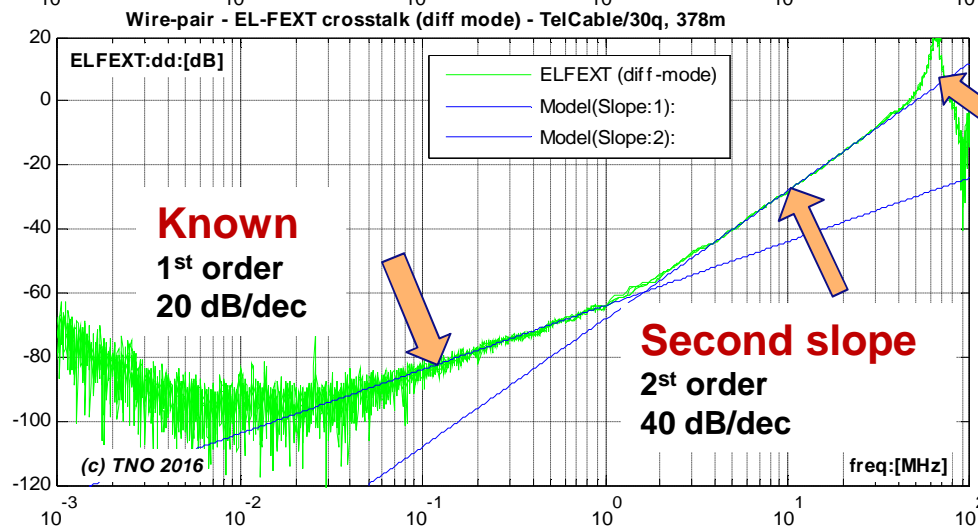
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# 1. FEXT crosstalk measurements in telephony cabling

An example: 30 quads, 378m, winded on a drum



- Why is 2<sup>nd</sup> order effect relevant for DSL?**
- Xtalk increases more rapidly with frequency
  - VDSL/35b and G.fast suffer from it
  - Dual slope effect not well understood
  - Model needed for performance predictions



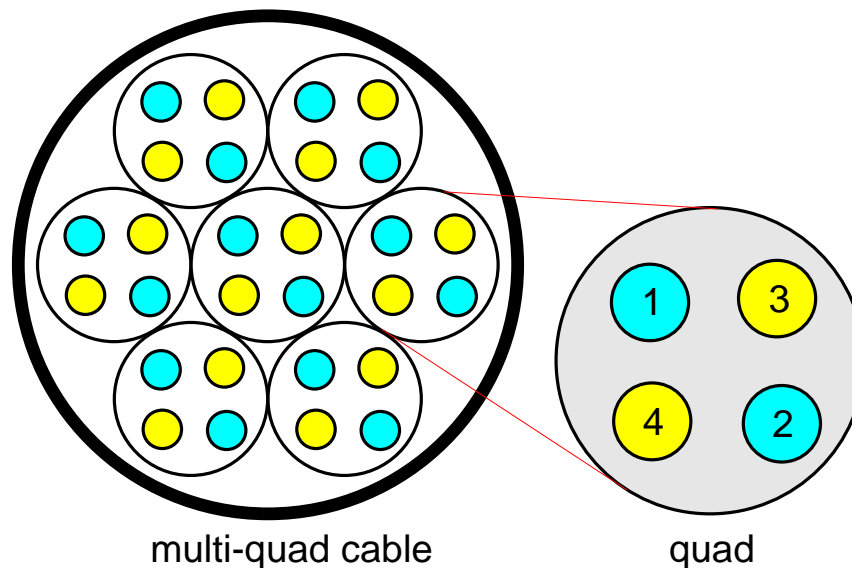
EL-FEXT > 0dB

Sudden increase of crosstalk (40 dB/decade)  
**“dual slope effect”**

# 1. FEXT crosstalk measurements in telephony cabling

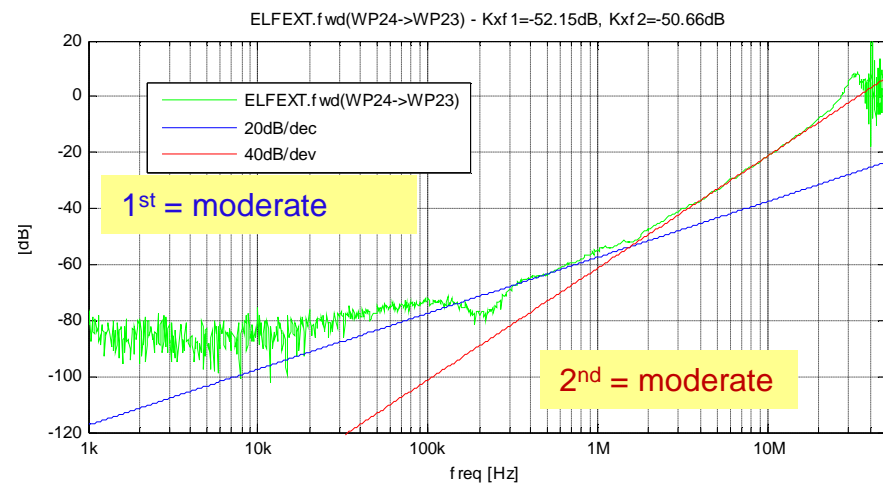
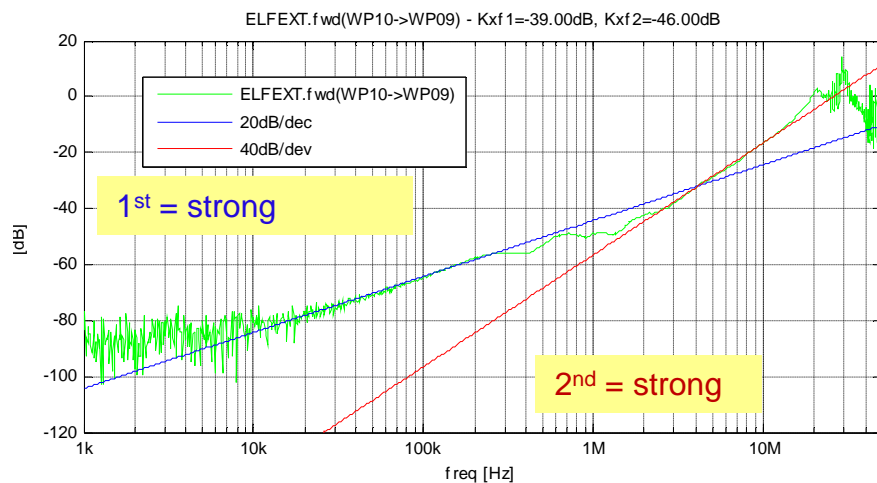
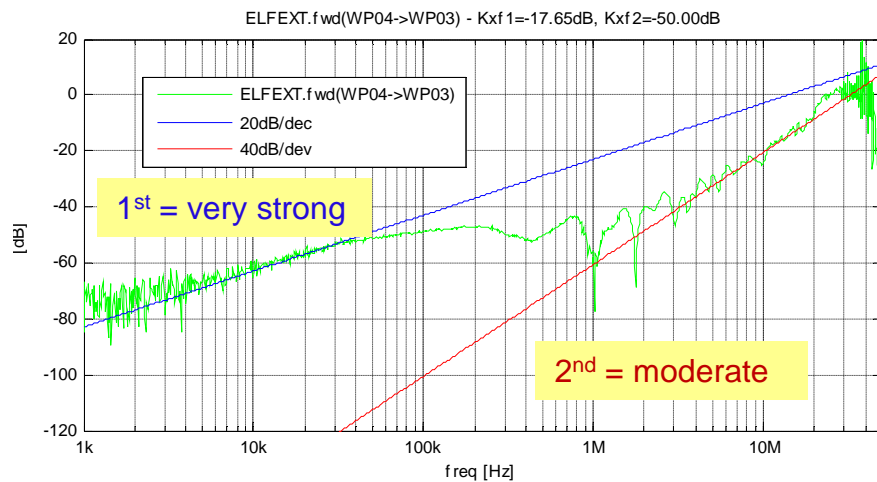
How behaves this dual-slope effect in other cables?

- 1<sup>st</sup> and 2<sup>nd</sup> order slopes are caused by independent mechanisms
- They scale differently with the cable length



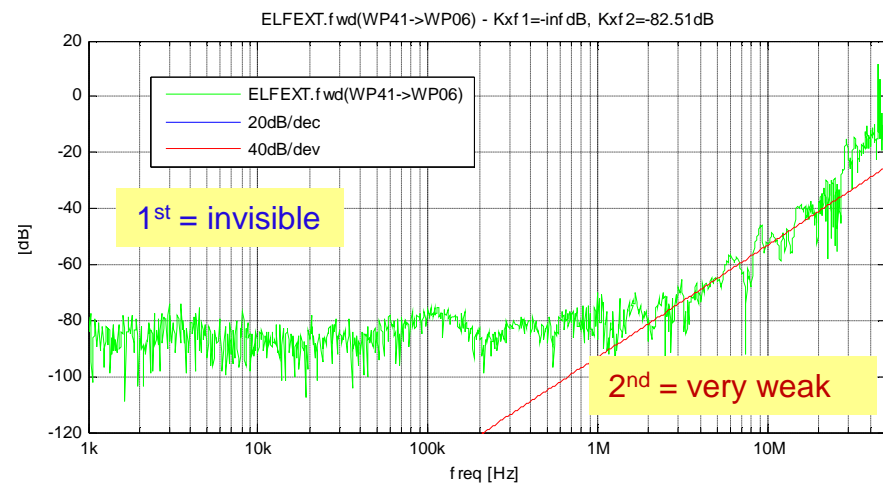
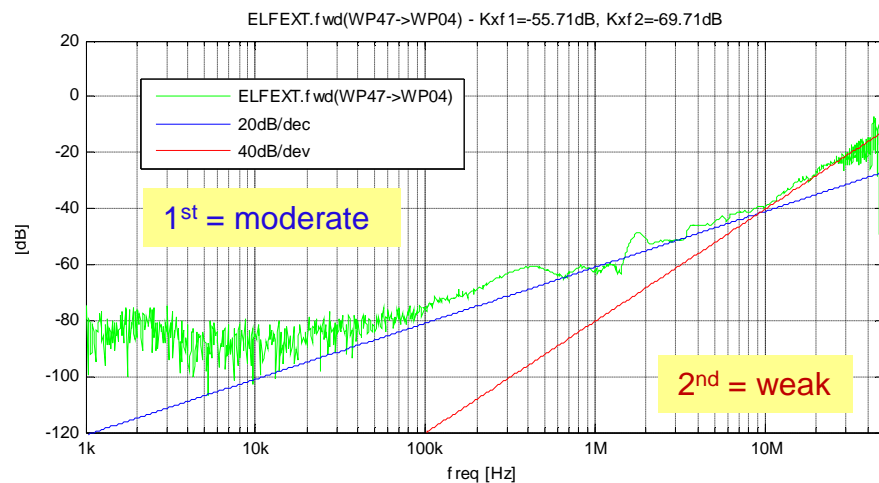
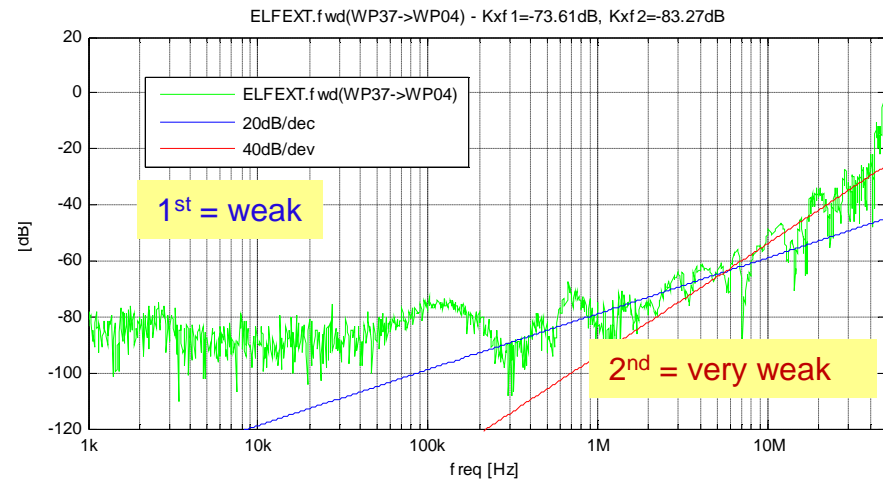
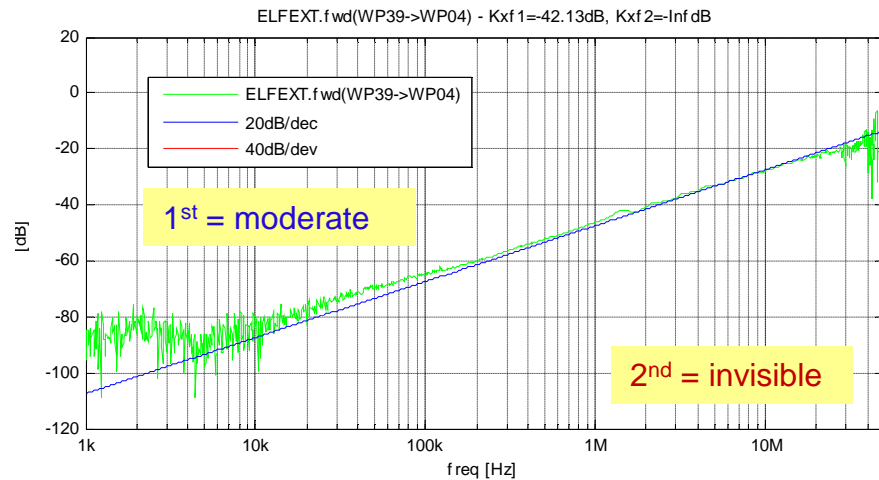
# 1. FEXT crosstalk measurements in telephony cabling

Other example: 280m, GPLK (paper insulated), drum, in-quad



# 1. FEXT crosstalk measurements in telephony cabling

Other example: 280m, GPLK (paper insulated), drum: **between quads**





# 1. FEXT crosstalk measurements in telephony cabling

Summary of observations so far

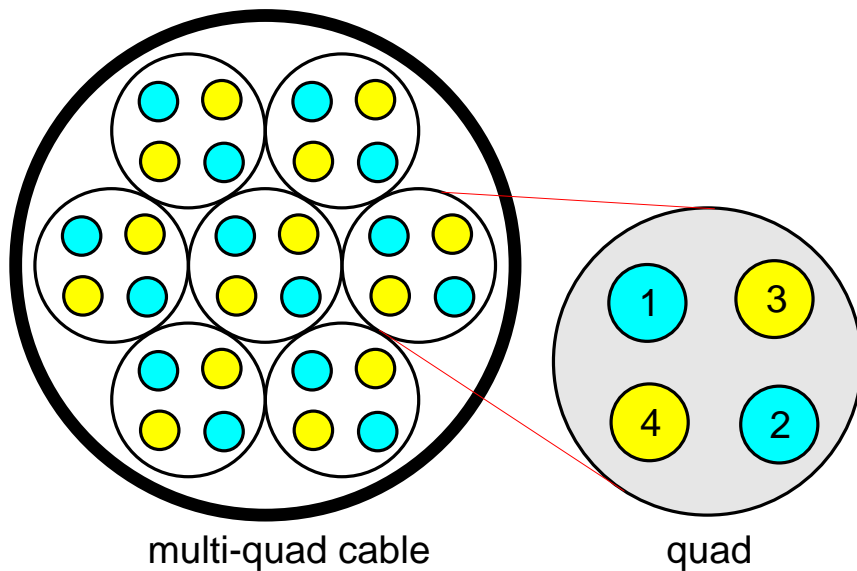
	In-quad	Between quads
1 <sup>st</sup> order crosstalk	Moderate à very strong	Invisible à moderate
2 <sup>nd</sup> order crosstalk	Moderate à strong	Invisible à weak

Observations so far:

- Crosstalk with mix of 1<sup>st</sup> and 2<sup>nd</sup> order effect
- Crosstalk with 1<sup>st</sup> order only (*2<sup>nd</sup> order invisible*)
- Crosstalk with 2<sup>nd</sup> order only (*1<sup>st</sup> order invisible*)
- 2<sup>nd</sup> order effect observed in both in-quad and between quads
- In-quad crosstalk more pronounced
  - à Dual slope more visible
  - à Lets focus on **in-quad** crosstalk to gain understanding

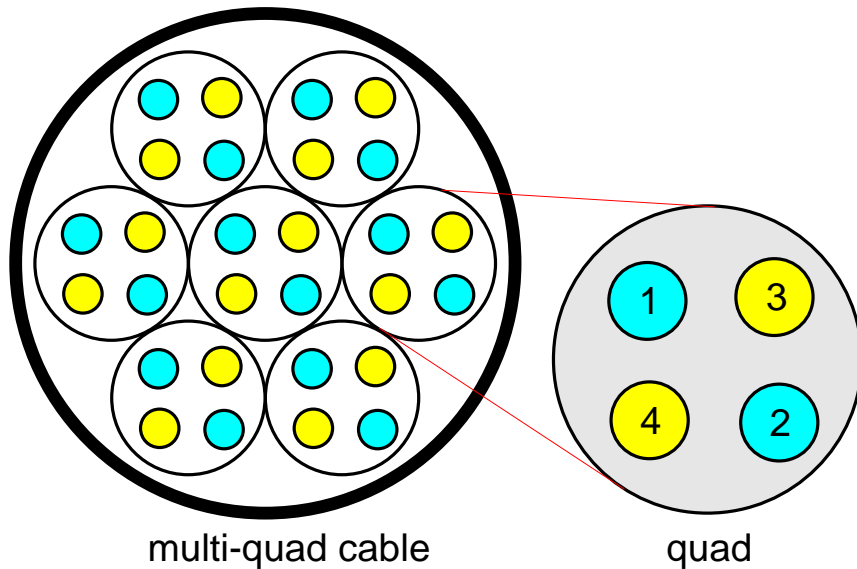
## 2. Understanding the cause of crosstalk

Cause of the **first** order effect (well known)

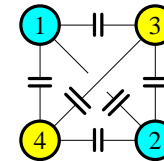


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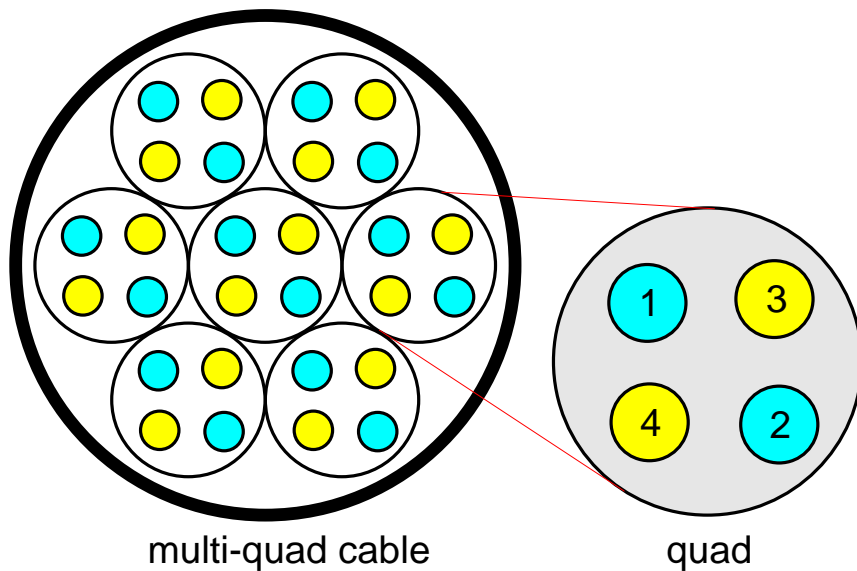
perfect square  
capacitive balance  
no crosstalk



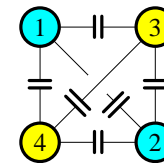
circuit equivalent

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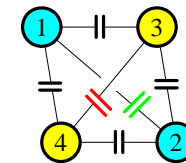


perfect square  
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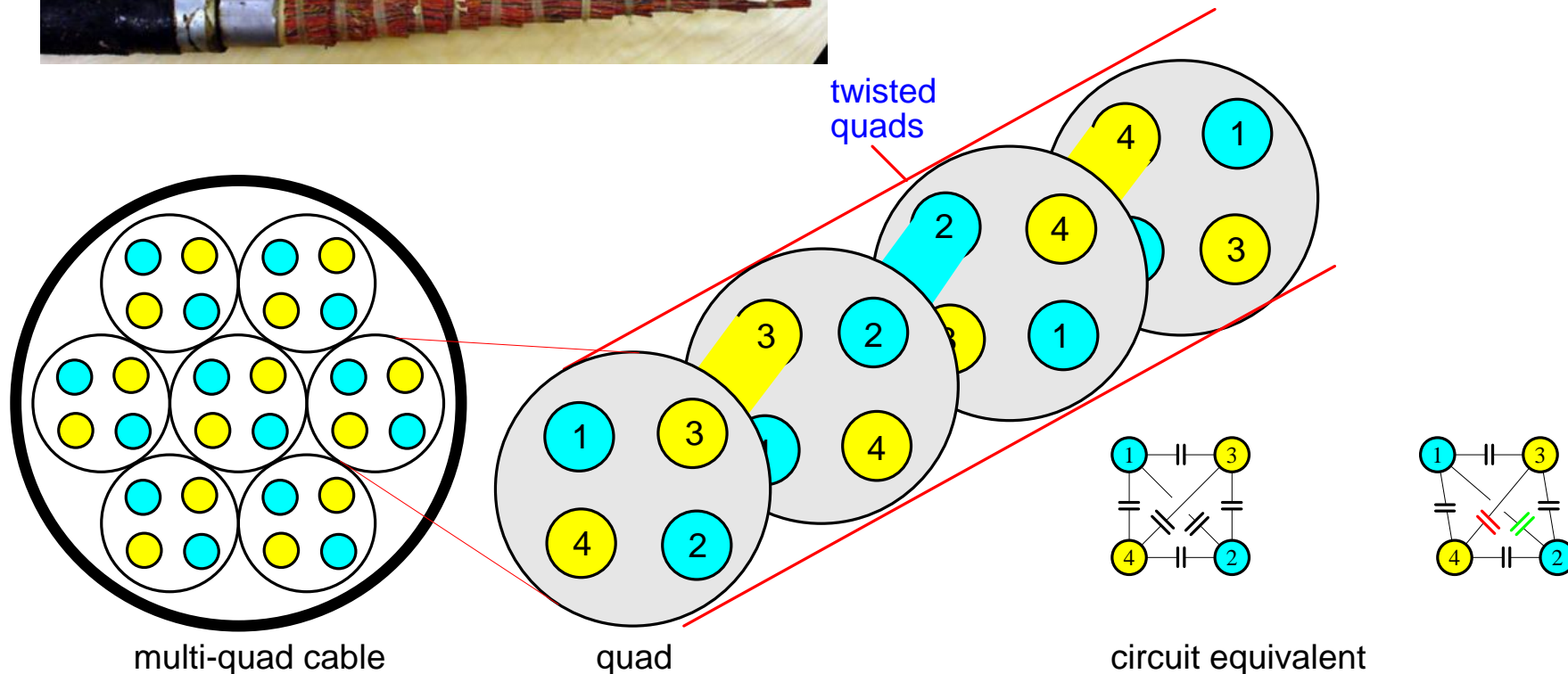
circuit equivalent

random variations  
small unbalance  
crosstalk



## 2. Understanding the cause of crosstalk

Cause of the **first** order effect (well known)



### Twisting can reduce crosstalk

- Does not reduce 1<sup>st</sup> order effect within a quad
- Reduces 1<sup>st</sup> order crosstalk between different quads
- Different quads should have different twist lengths

## 2. Understanding the cause of crosstalk

Cause of the **first** order effect (well known)



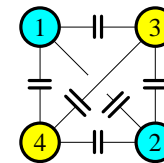
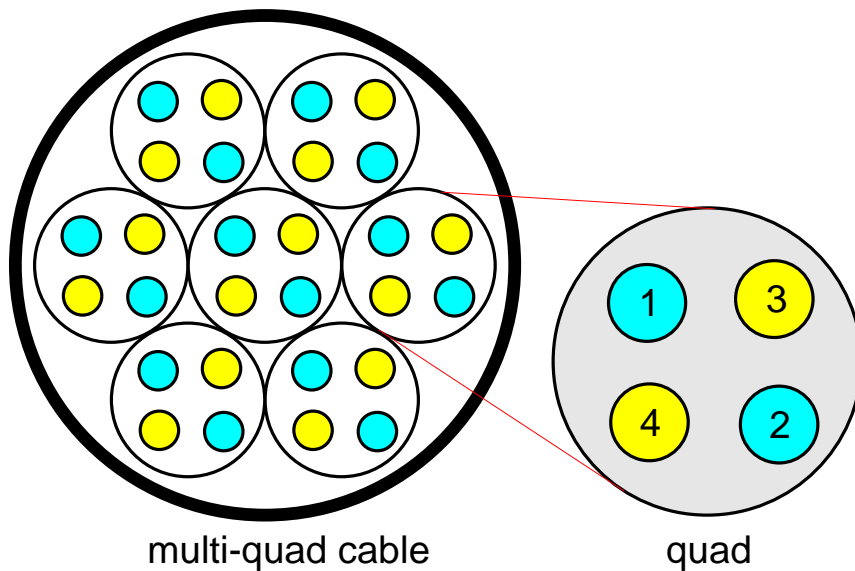
First order effect of EL-FEXT (well known):

- **Random perturbation** of balance by imperfect geometry
- Scales proportionally with frequency (20 dB/decade)
- Scales with the root of the cable length ( $\sqrt{L}$ )

Bell technical staff, *Transmission Systems for Communications*,  
Bell Telephone Laboratories,  
1969 (1<sup>st</sup> ed 1954)

## 2. Understanding the cause of crosstalk

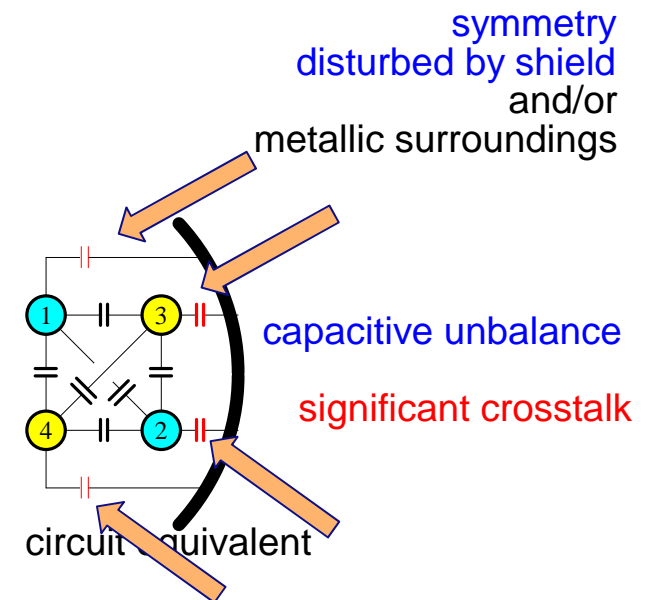
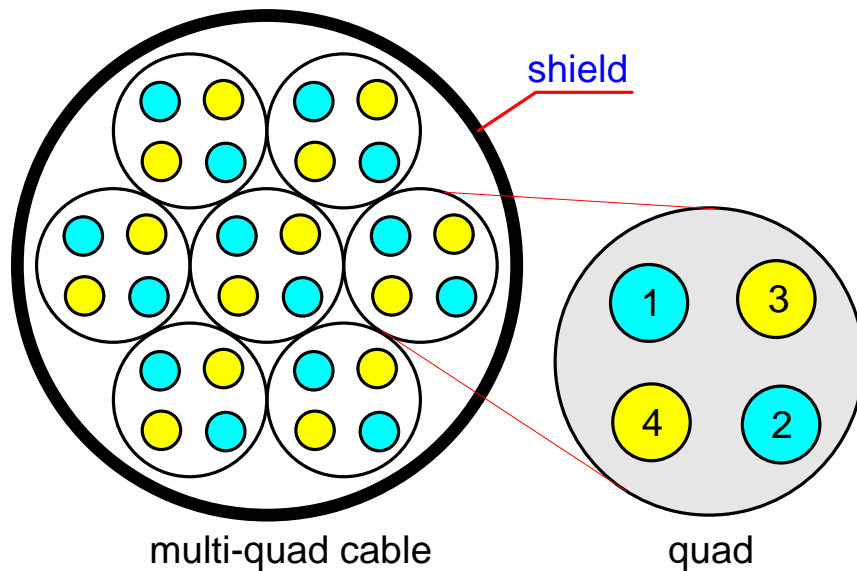
Cause of the **second** order effect



circuit equivalent

## 2. Understanding the cause of crosstalk

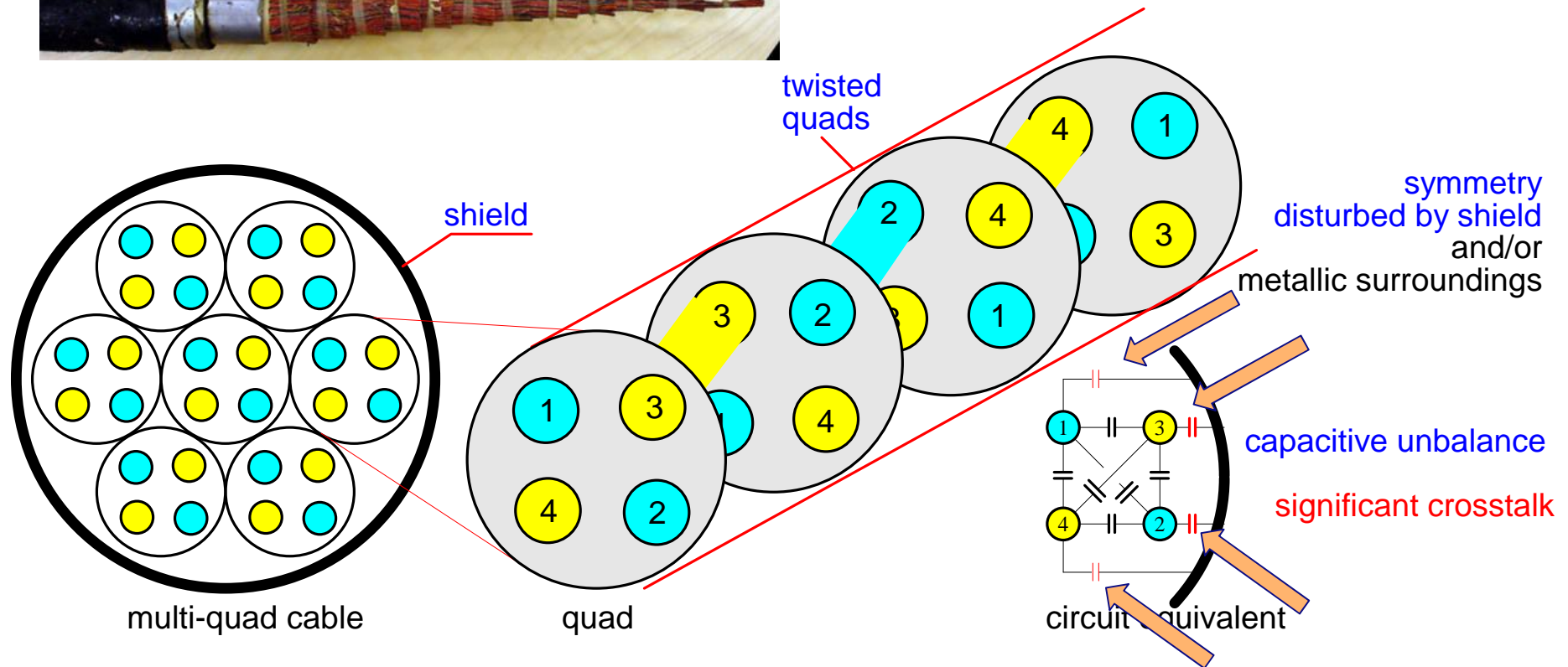
Cause of the **second** order effect





## 2. Understanding the cause of crosstalk

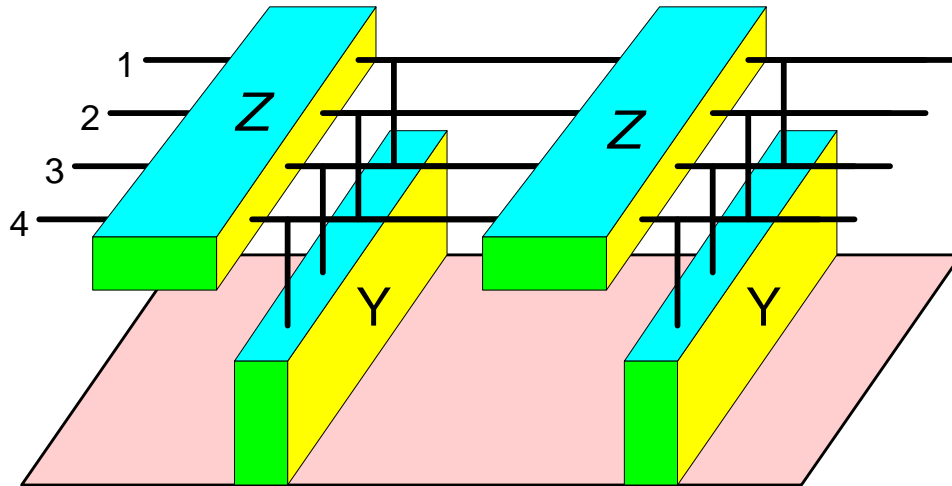
Cause of the **second** order effect



Twisting a quad restores capacitive balance only on average  
 Significant crosstalk reduction within the quad  $\hat{=}$  residual crosstalk  
 Tighter twisting of a quad  $\hat{=}$  lowers residual crosstalk (= 2<sup>nd</sup> order effect)

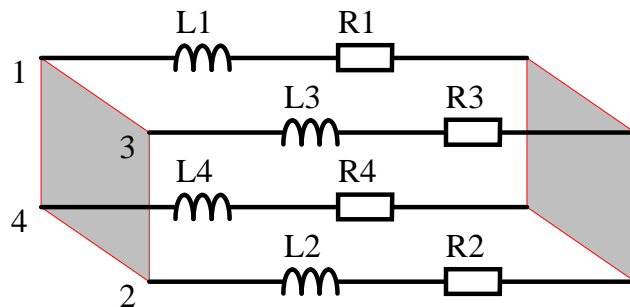
### 3. Brute force modelling crosstalk within a quad

Four wires and a shield = eight port

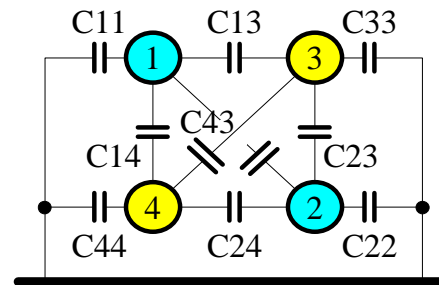


$$\frac{\partial}{\partial z} \mathbf{U}(z) = -\mathbf{Z}_s \cdot \mathbf{I}(z)$$

$$\frac{\partial}{\partial z} \mathbf{I}(z) = -\mathbf{Y}_p \cdot \mathbf{U}(z)$$



Z

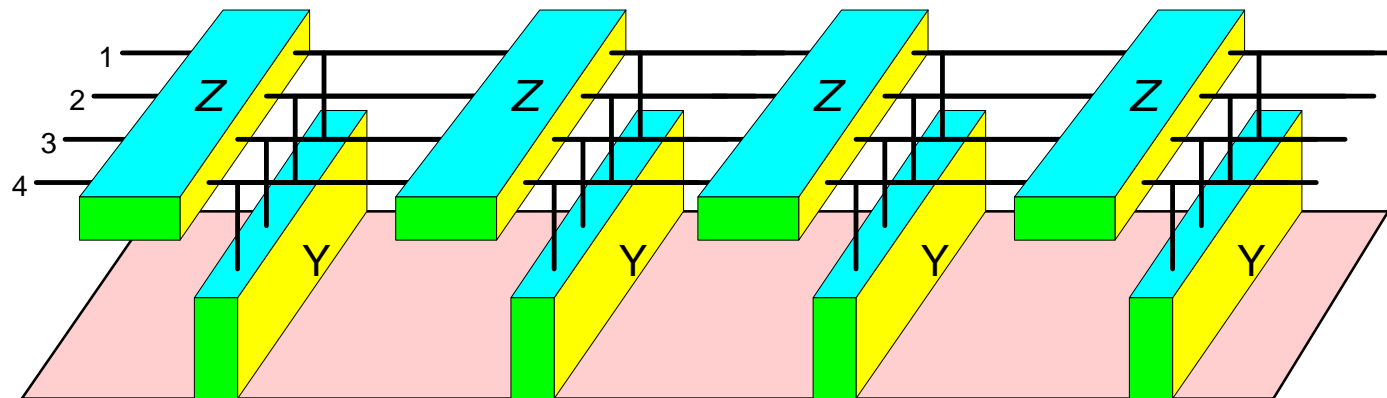


Y

Clayton R. Paul, *Analysis of multiconductor transmission lines*, IEEE press, 2008

### 3. Brute force modelling crosstalk within a quad

“Infinite” cascade  $\rightarrow$  eight port cable model

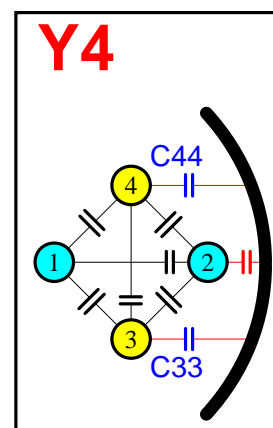
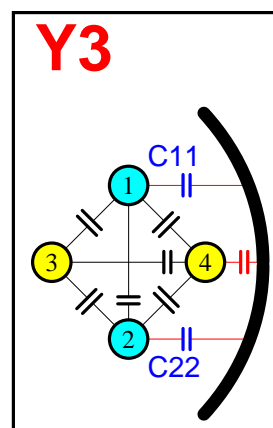
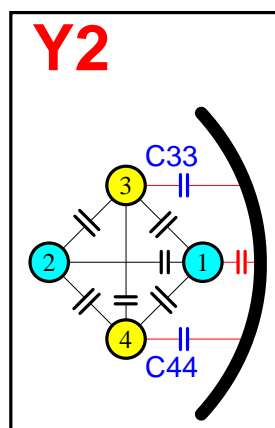
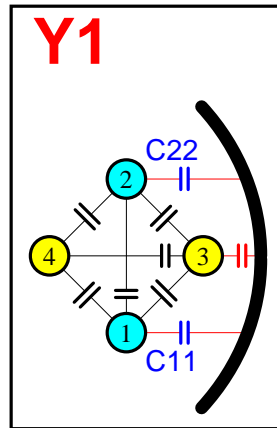
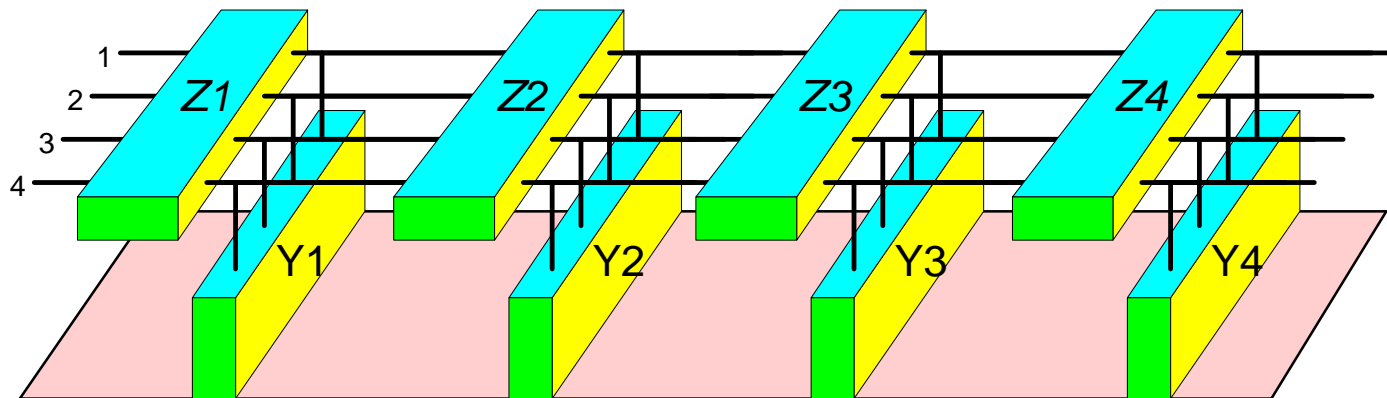


**With only 9 values (for R,L,C) you can  
do a very good cable simulation .....**

**.... but the dual slope effect will not be  
visible**

### 3. Brute force modelling crosstalk within a quad

“Infinite” cascade → eight port cable model → adding a twist



Cascade of piecewise uniform segments can add the **twist** to the cable

**4 sections/twist ?**  
**16 sections/twist ?**  
**64 sections/twist ?**

$$\begin{aligned} C_{11} &= C_c \\ C_{22} &= C_c \\ C_{33} &= C_c + dC \\ C_{44} &= C_c - dC \end{aligned}$$

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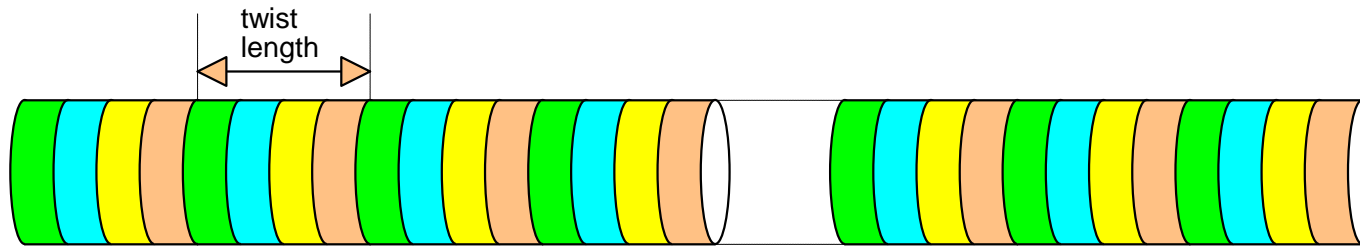
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$$\begin{aligned} C_{11} &= C_c / (1 + \Delta_c \cdot \sin(2p \cdot k/n \cdot \Delta L)) \\ C_{22} &= C_c / (1 - \Delta_c \cdot \sin(2p \cdot k/n \cdot \Delta L)) \\ C_{33} &= C_c / (1 + \Delta_c \cdot \cos(2p \cdot k/n \cdot \Delta L)) \\ C_{44} &= C_c / (1 - \Delta_c \cdot \cos(2p \cdot k/n \cdot \Delta L)) \end{aligned}$$

### 3. Brute force modelling crosstalk within a quad

“Infinite” cascade à eight port cable model



**Twist length = 3 cm**  
**Cable length = 300m**  
**Model with 4 segments per twist**

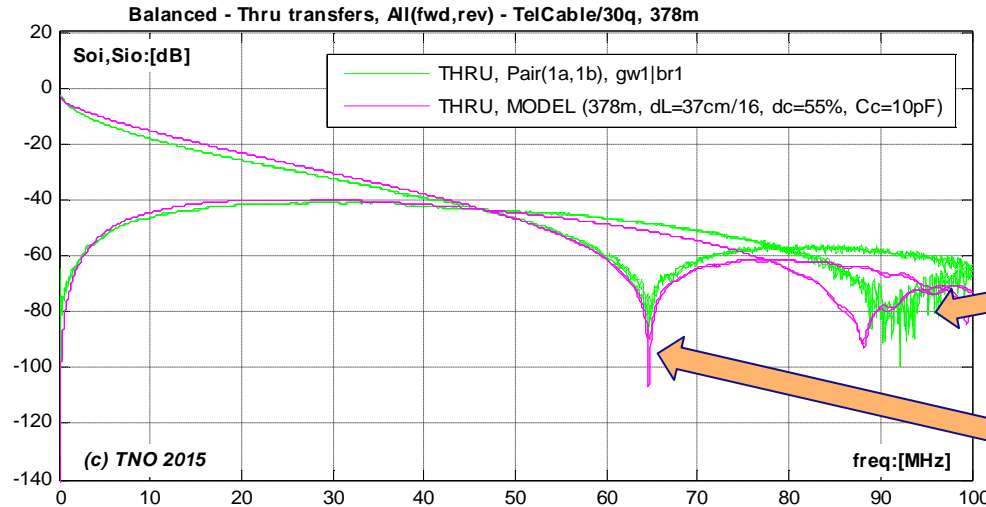
à 10000 twists in a cable  
à 40000 segments in a cable  
à And they all should go in the cascade

**That was the theory,**

**But is it also realistic,  
and is it good enough?**

### 3. Brute force modelling crosstalk within a quad

Match between model and measurement



**Very good match** between model and measurement

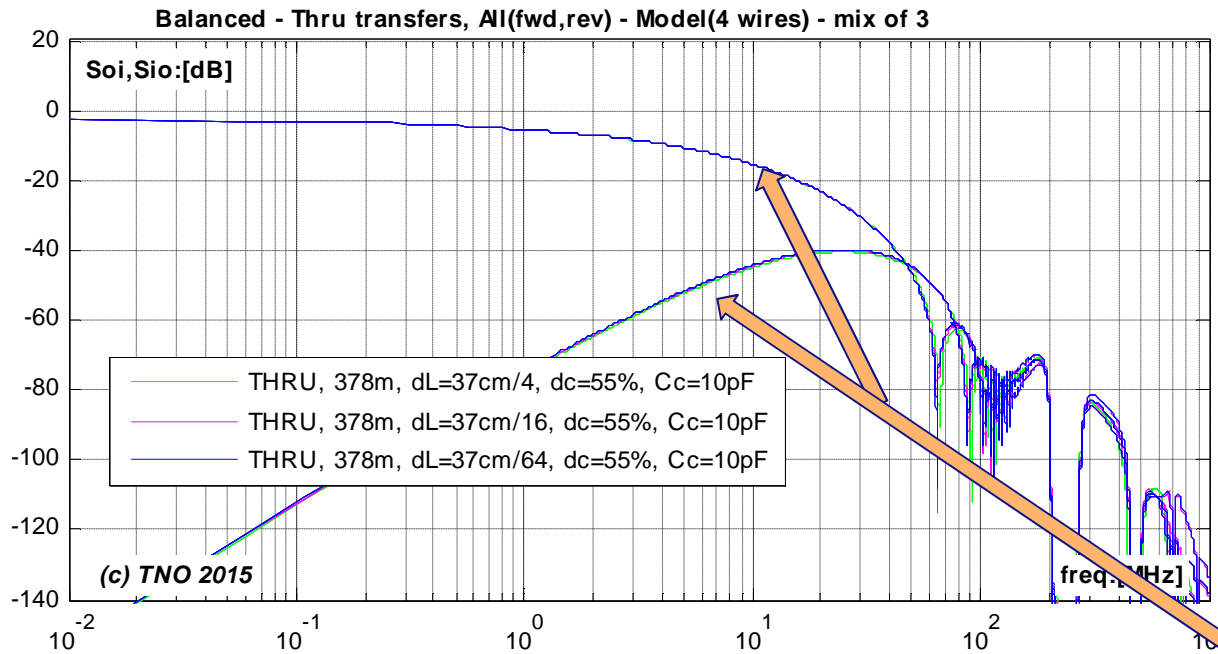
This error is because we ignored that insulator has a frequency dependency

Even the dip is well modelled



### 3. Brute force modelling crosstalk within a quad

How many segments per twist are needed for a good match?



Three different simulation runs ...

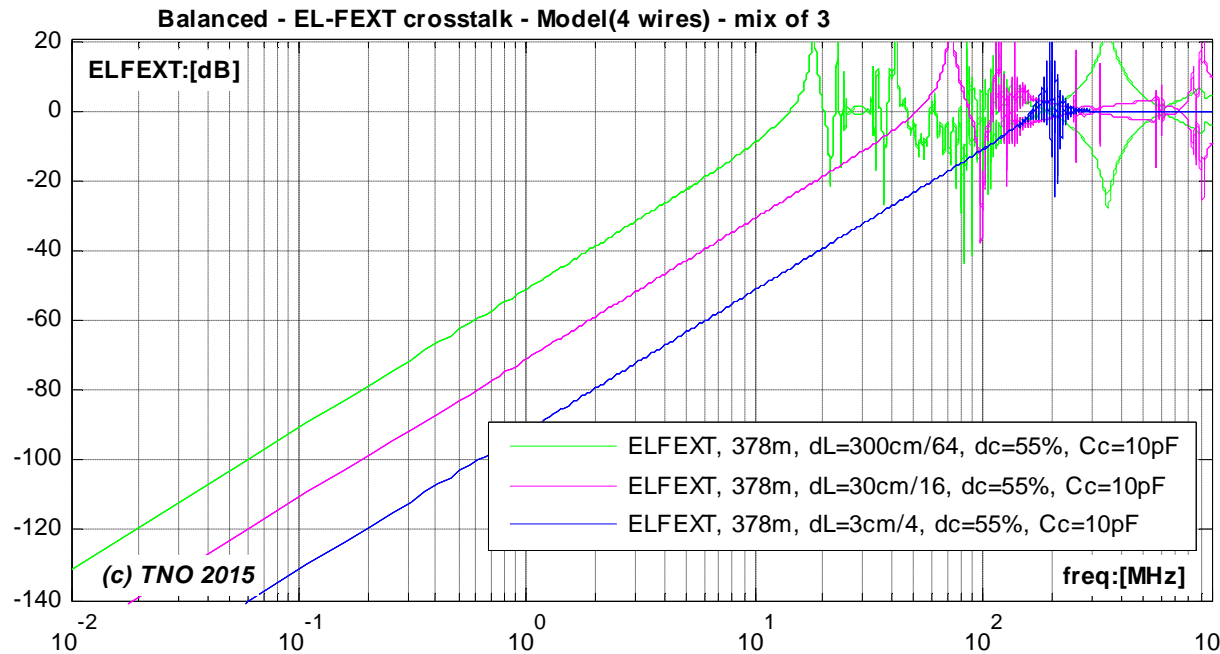
With different segments/twist  
 4 segments/twist  
 16 segments/twist  
 64 segments/twist

You cannot see the difference!

4 segments/twist appears to be enough!

### 3. Brute force modelling crosstalk within a quad

Dual slope effect, as a function of the twist length



Three different simulation runs

With different twist lengths  
**300 cm**  
**30 cm**  
**3 cm**

EL-FEXT has 40 dB slope (**second order effect**)

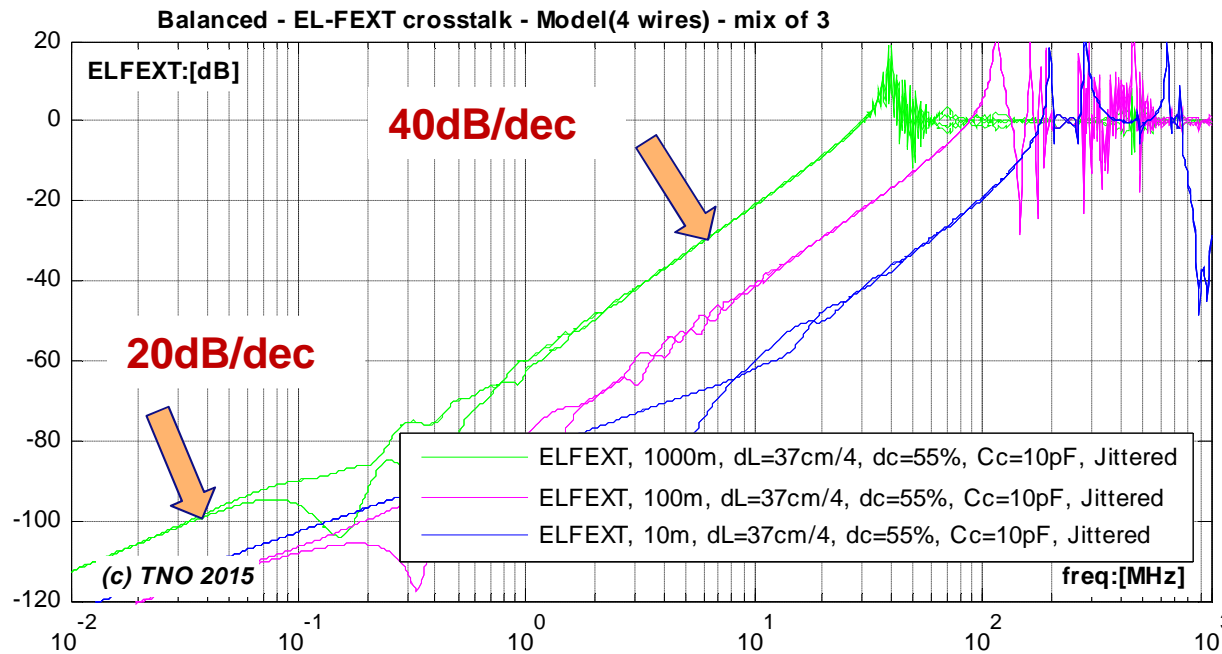
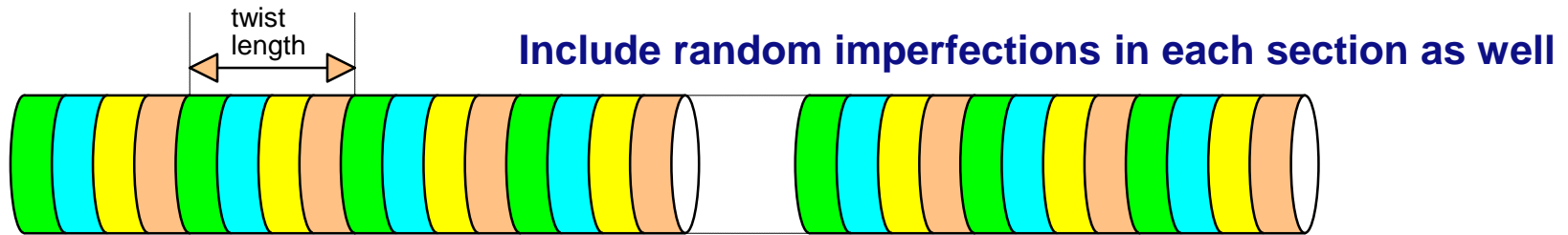
Even when all random perturbations (**first order effect**) is absent

An decrease of the twist length by a factor 10 ...  
 ... decreases the EL-FEXT by 20 dB (**second order effect**)



### 3. Brute force modelling crosstalk within a quad

Fair prediction as function of frequency and cable length for both the first **and** second order effects!



Three different simulation runs

Changing the loop length

10m  
100m  
1000m

### 3. Brute force modelling crosstalk within a quad

Cause of the **first** and **second** order effect (well known)



First order effect of EL-FEXT (well known):

- **Random perturbation** of balance by imperfect geometry
  - Scales proportionally with frequency (20 dB/decade)
  - Scales with the root of the cable length ( $\sqrt{L}$ )
- (only on a statistical sense)*

Second order effect of EL-FEXT

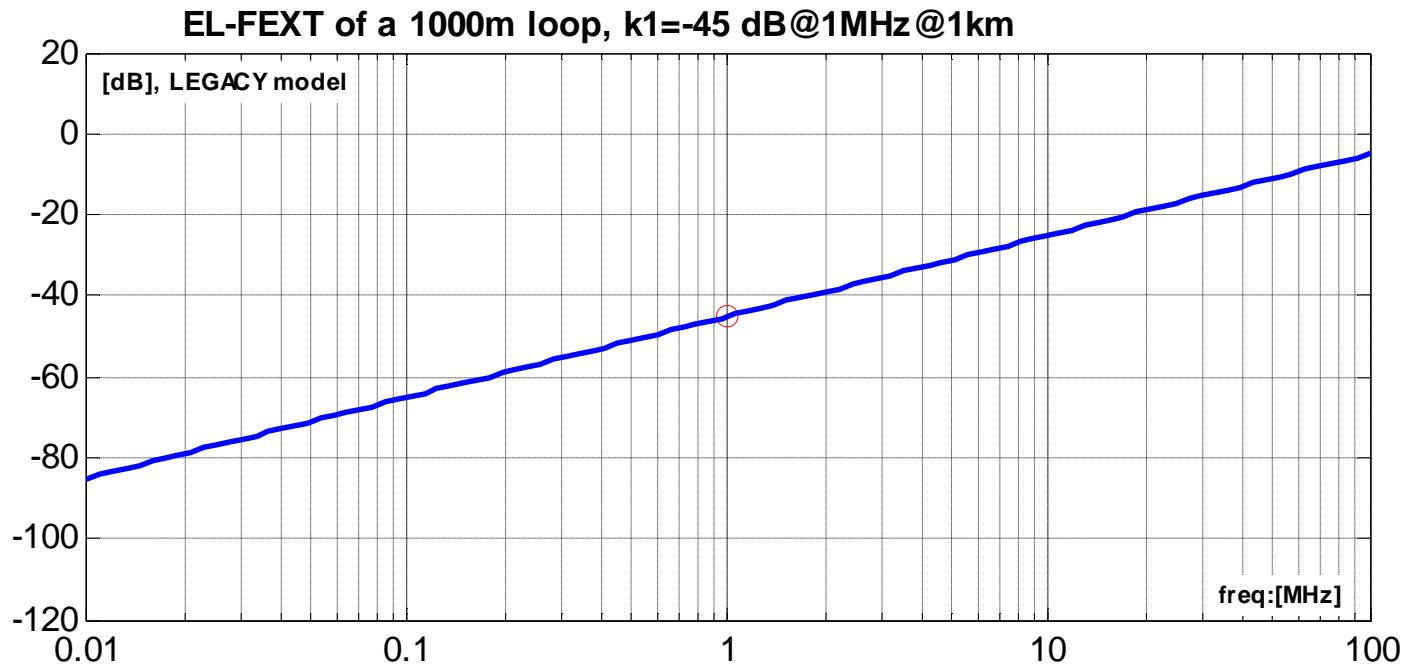
- **Deterministic perturbation** of balance by metallic surroundings
- Scales proportionally with square of frequency (40 dB/decade)
- Scales with the cable length (L)

## 4. Simplifying the system model on EL-FEXT

Fair prediction as function of frequency and cable length

Legacy system model for EL-FEXT (first order only, ETSI TR 101 830-2)

- **First order slope of 20 dB/decade**
- **Scales with the root of cable length**
- **No second order slope**
- **Infinite high EL-FEXT at high frequencies**

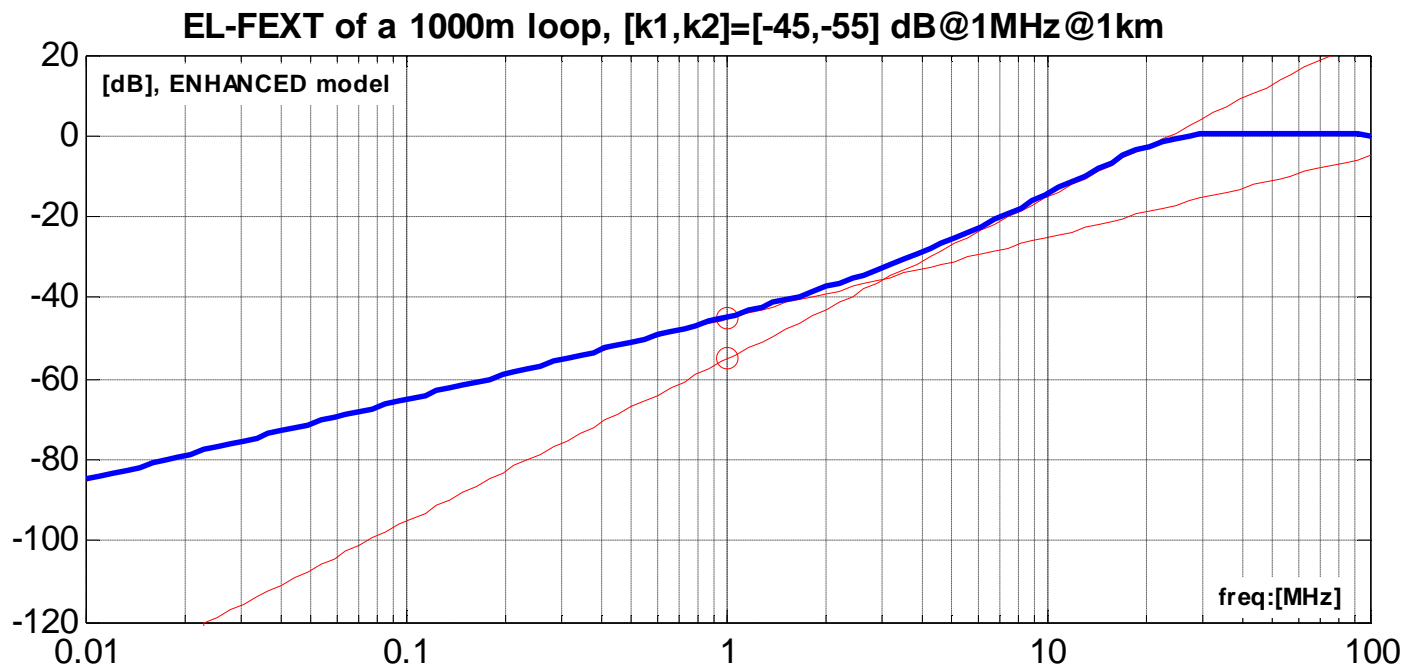


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Fair prediction as function of frequency and cable length

### Enhanced system model for EL-FEXT (first + second order)

- **First order slope of 20 dB/decade**
- **Second order slope of 40 dB/decade**
- **Does not exceed 0dB for high frequencies**
- **First order slope scales with the root of cable length**
- **Second order slope scales linear with the cable length**

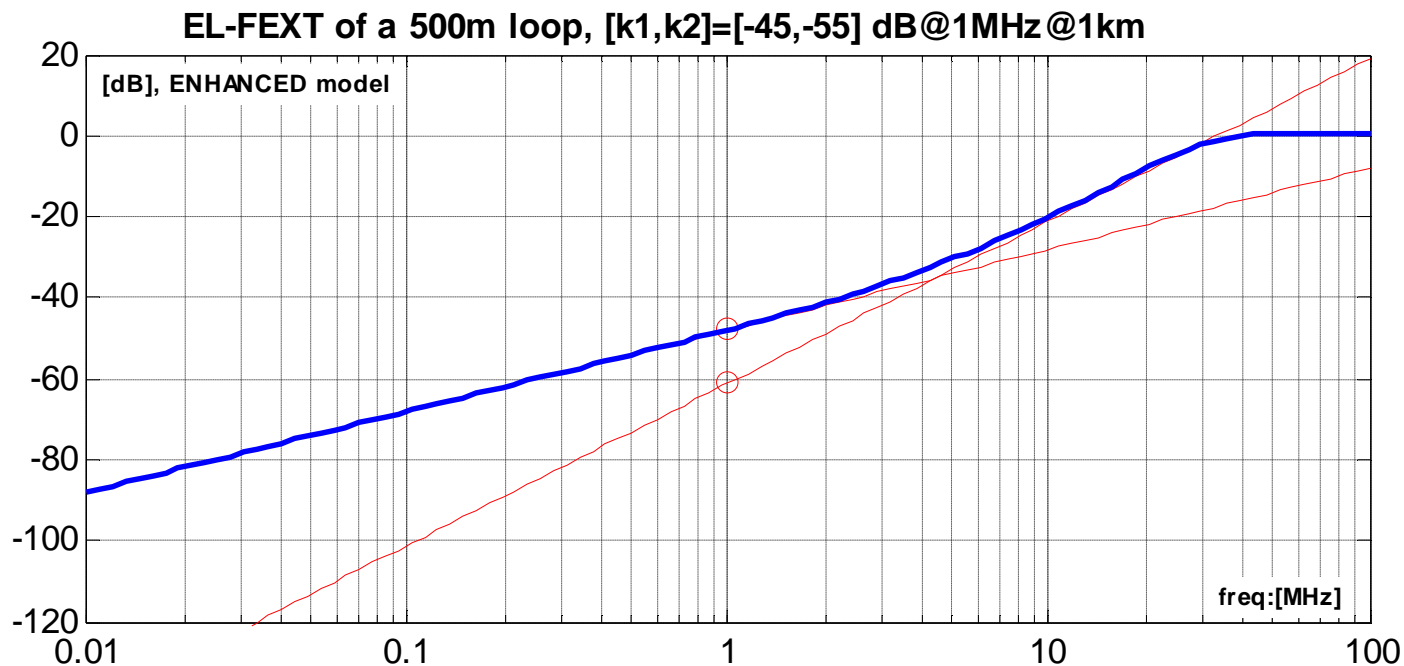


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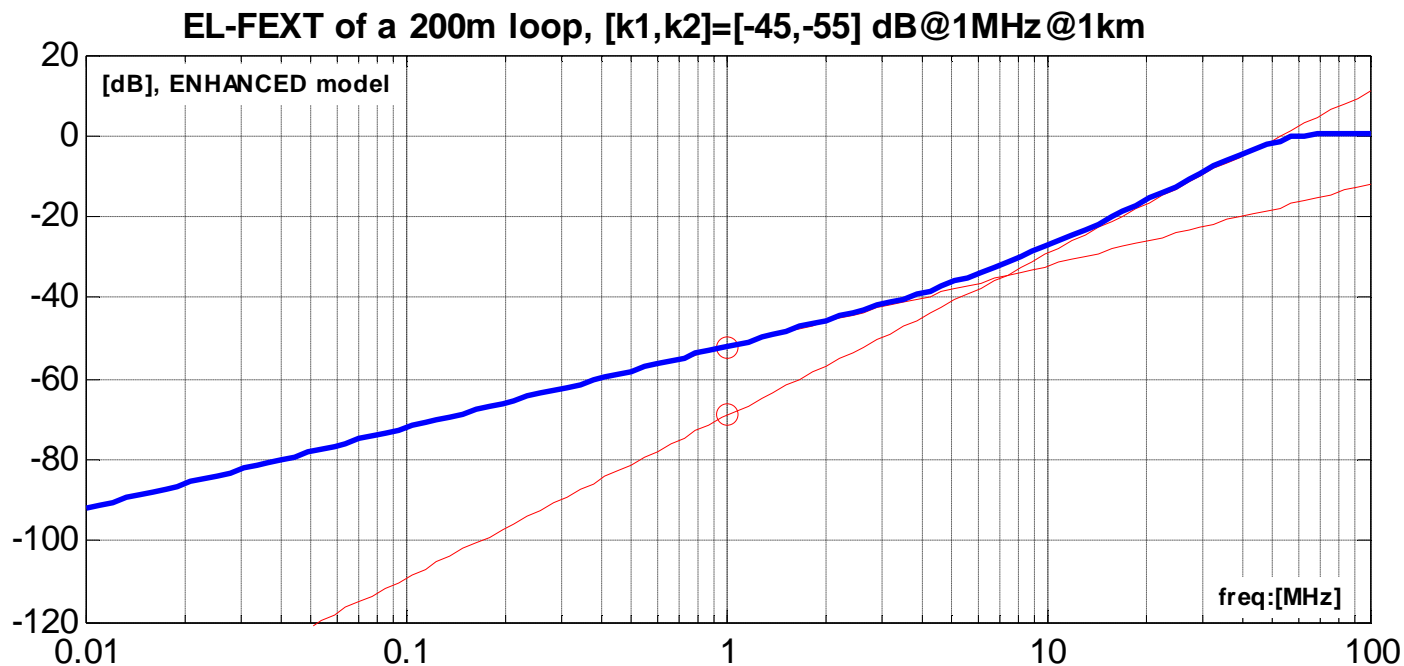


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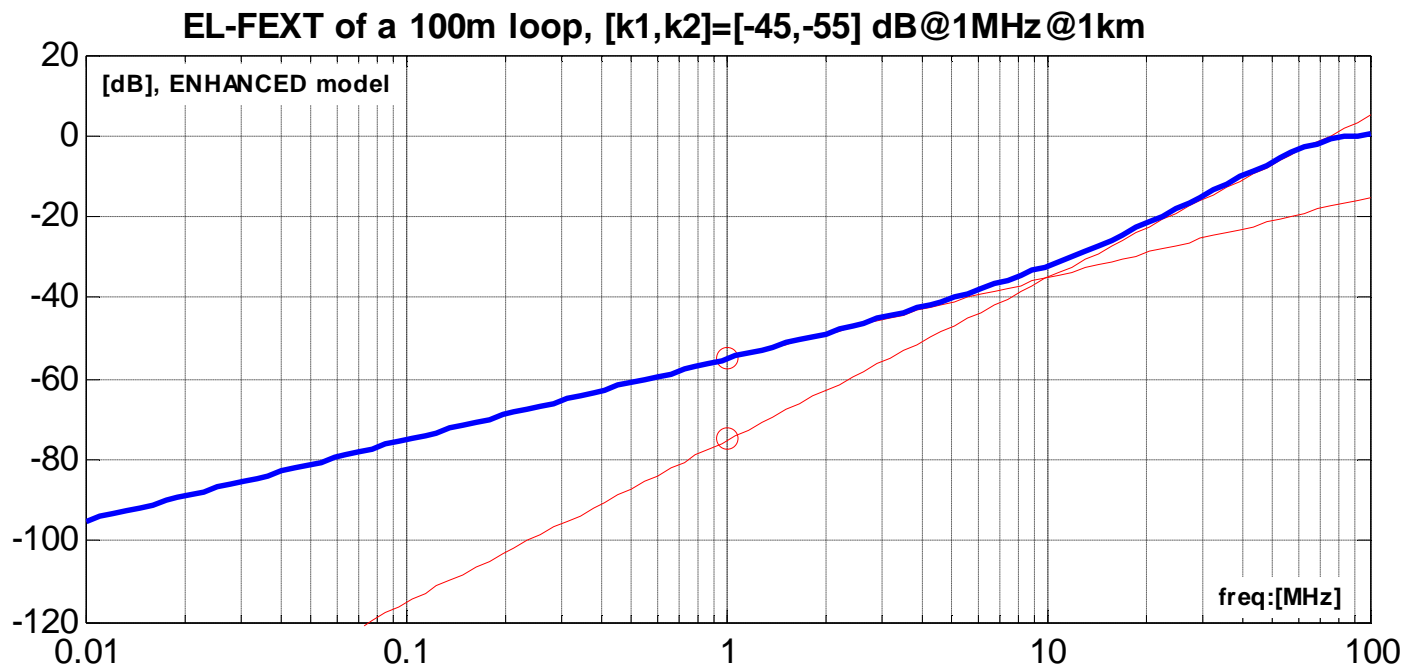


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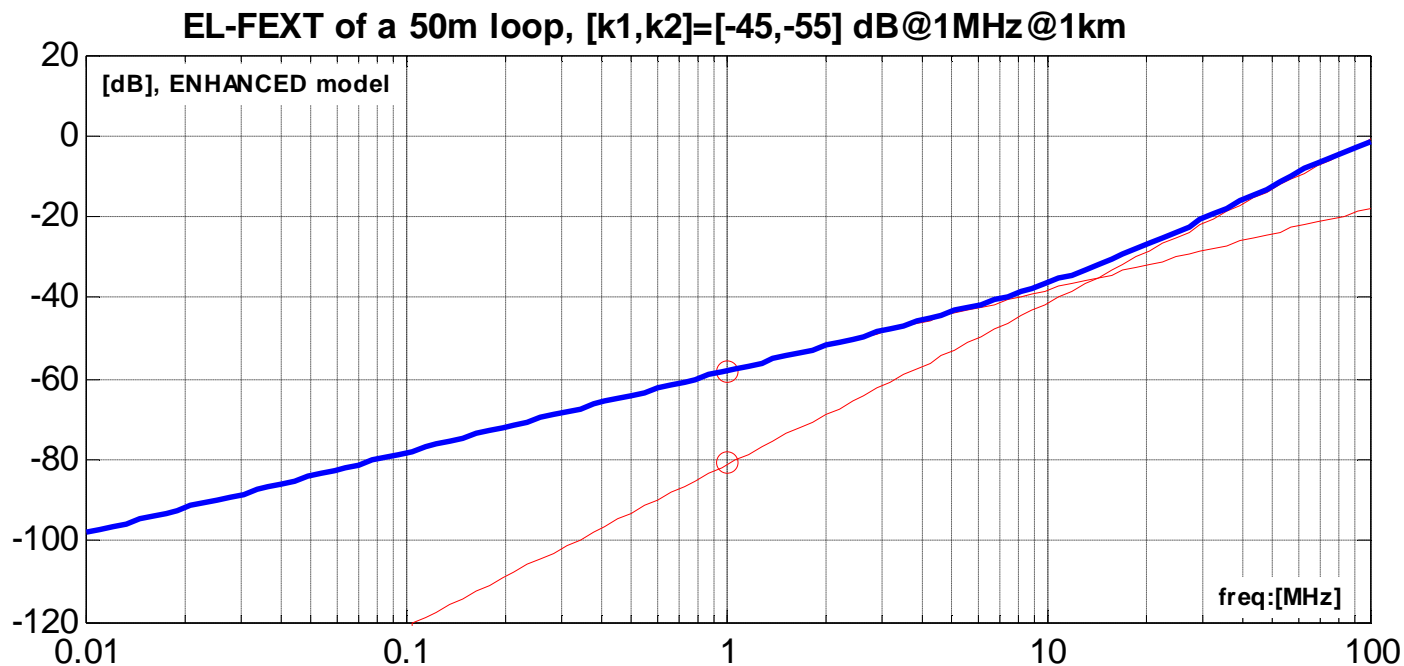


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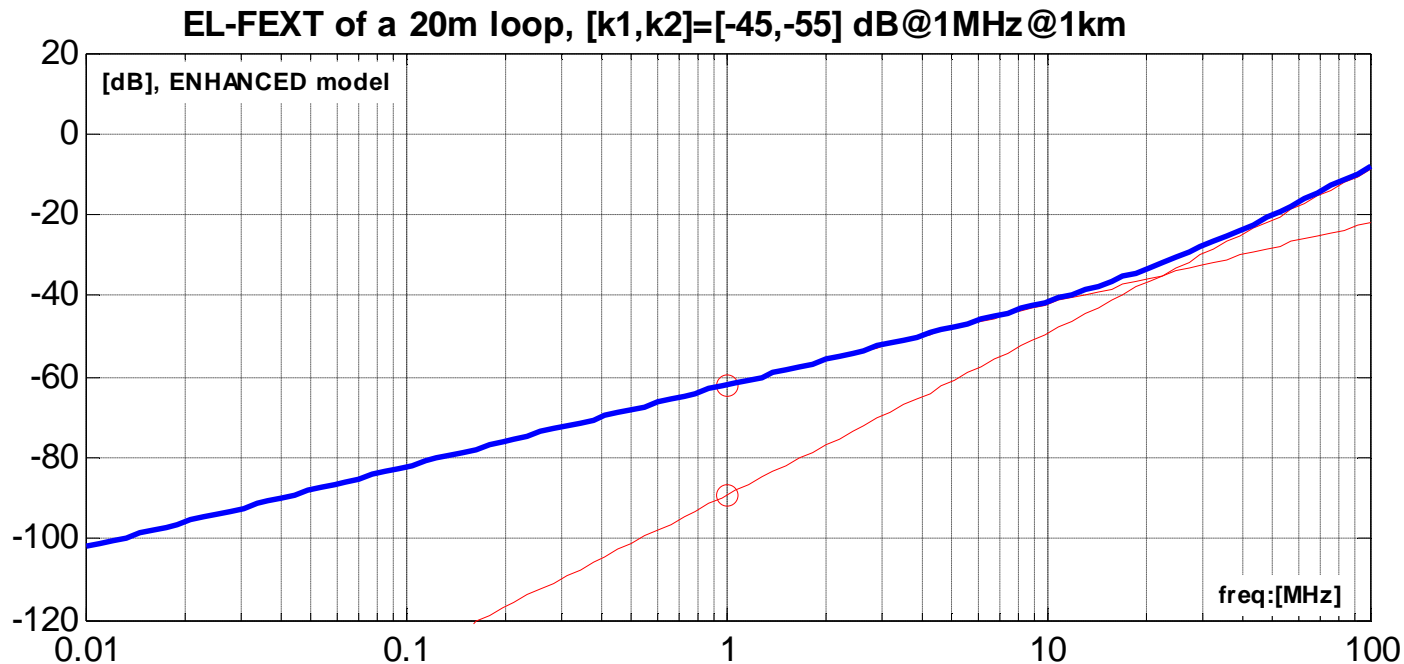


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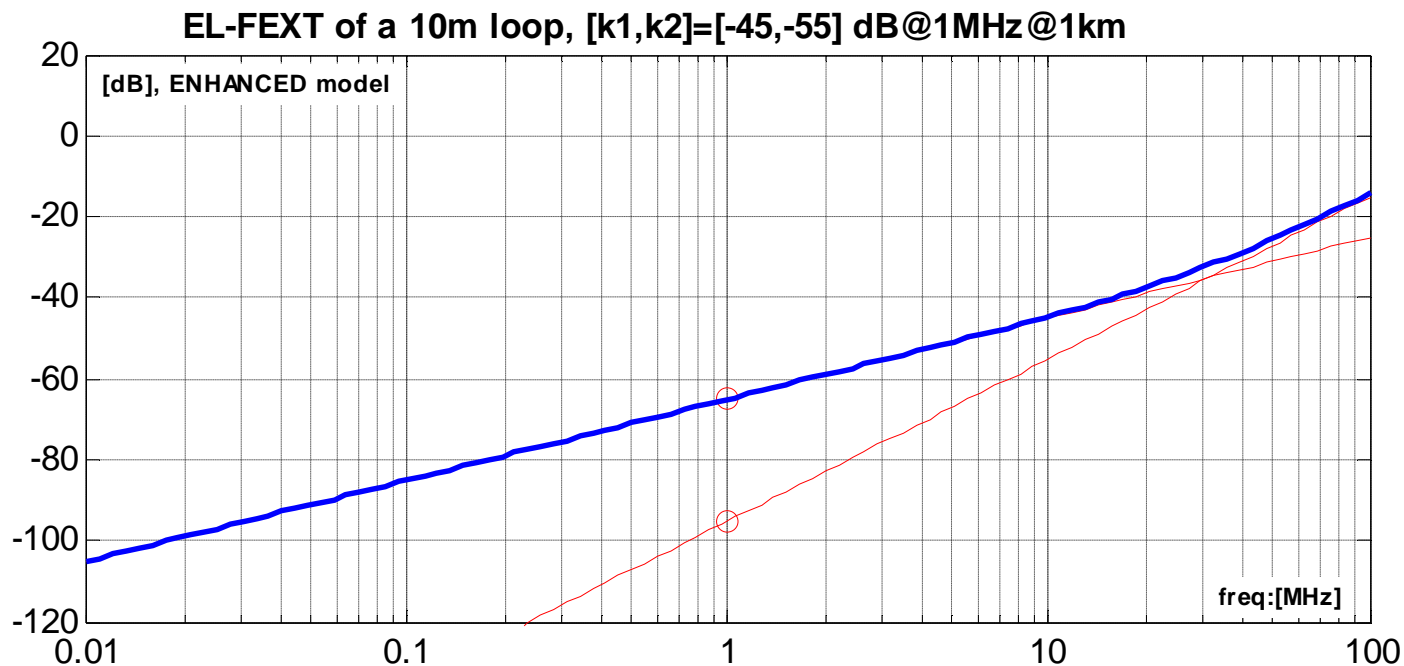


## 4. Simplifying the system model on EL-FEXT

Fair prediction as function of frequency and cable length

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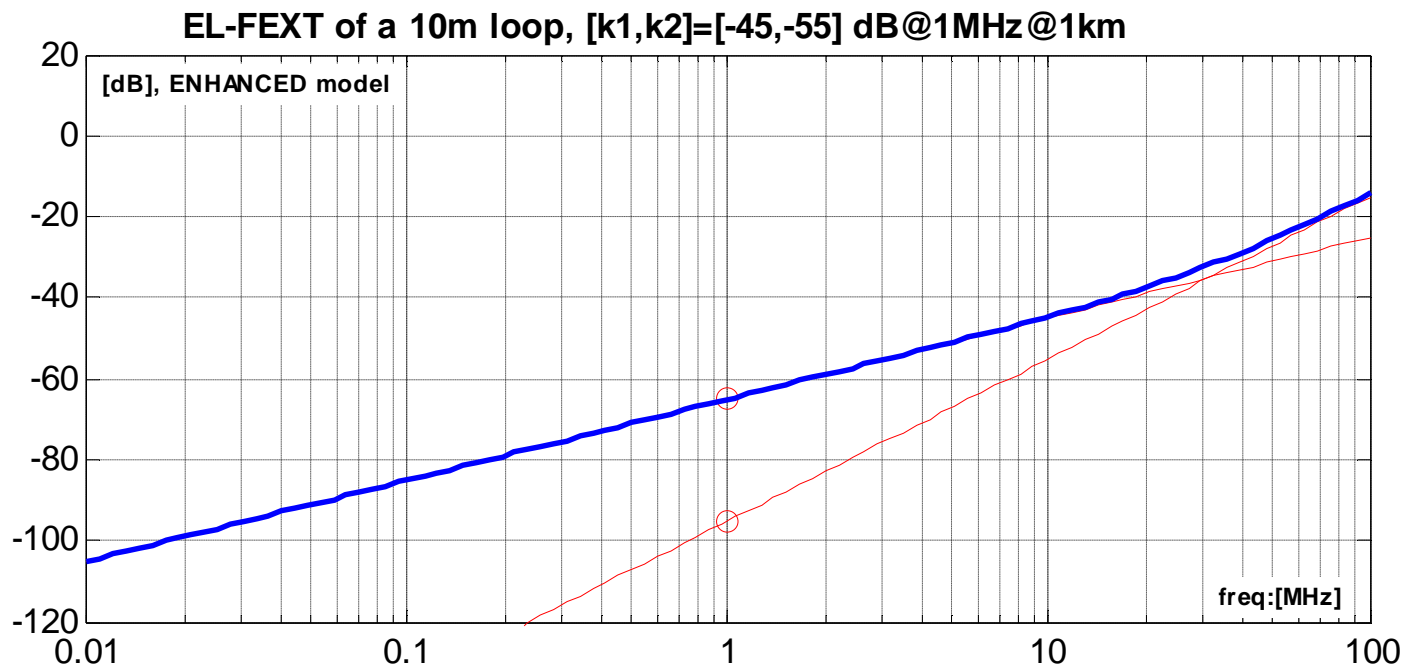
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A second order high-pass filter curve meets all these requirements



# 4. Simplifying the system model on EL-FEXT

Fair prediction as function of frequency and cable length

## Enhanced model for EL-FEXT (first + second order)

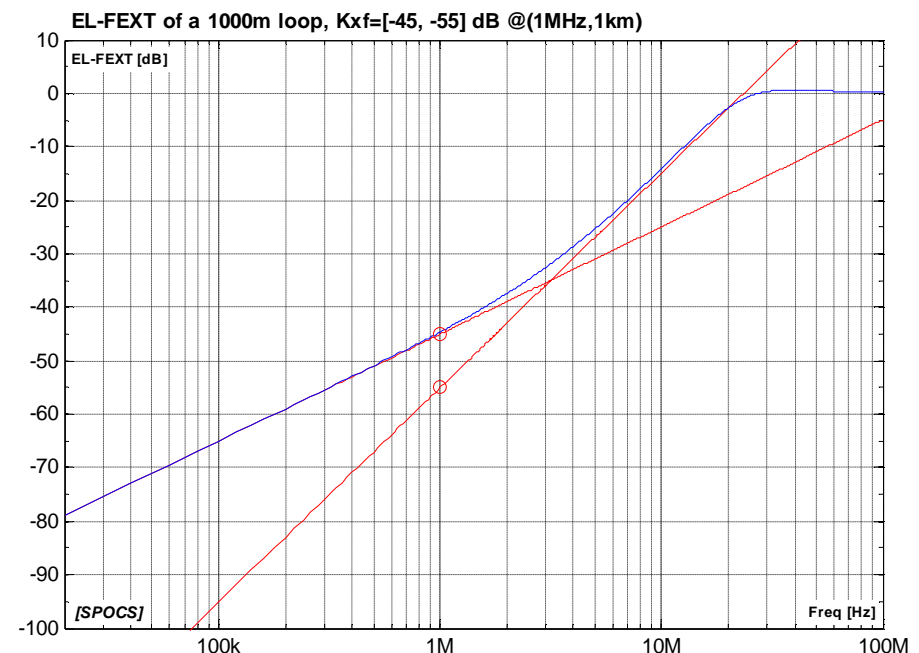
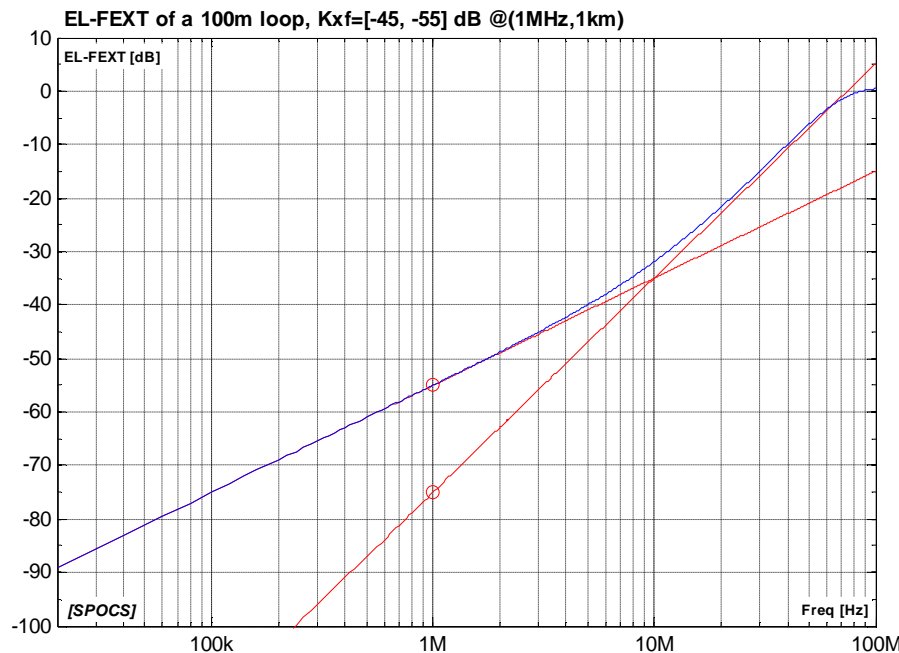
$$H_{ELFEXT}(j\omega, L) = \left\| \frac{k_1(L) \cdot \left(\frac{j\omega}{\omega_0}\right) + k_2(L) \cdot \left(\frac{j\omega}{\omega_0}\right)^2}{1 + \left(k_1(L) + \sqrt{k_2(L)}\right) \cdot \left(\frac{j\omega}{\omega_0}\right) + k_2(L) \cdot \left(\frac{j\omega}{\omega_0}\right)^2} \right\|$$

e.g.

$K_{XF1} = -45\text{dB} \text{ (@1MHz, 1km)}$

$K_{XF2} = -55\text{dB} \text{ (@1MHz, 1km)}$

where  $k_1(L) = K_{XF1} \cdot \sqrt{L/L_0}$ , and  $k_2(L) = K_{XF2} \cdot (L/L_0)$



# 5. Conclusions

Discussed the dual slope effect in crosstalk (EL-FEXT)

- EL-FEXT increases more rapidly at higher frequencies (40 dB/decade):
  - Dual slope effect in EL-FEXT raised in ITU, Feb 2012 (2012-04-4A-038)
  - Confirmed by many measurements in different labs.
  - Has an impact on both G.fast and VDSL performance (above a few MHz)
  - Vector engines should cope with it.
  
- Achieved a good understanding on the origin of this effect:
  - Derived via an advanced brute force multi-port model of a cable (L,C,R)
  - 2<sup>nd</sup> order effect due to *deterministic* interaction of twist in quads and their metallic surroundings
  - 1<sup>st</sup> order effect due to *random* perturbation in geometry
  - Both effects are independent from each other
  - Both effects scale differently with cable length
  - Details in IEEE paper (submitted in Jan & May 2016)
  
- Proposed a simple FEXT model for performance simulations:
  - Simple extension to legacy crosstalk model (ETSI)
  - Handles magnitude (both slopes) and length scaling quite well
  - Convenient for performance simulations on VDSL & G.fast
  - Contributed to ITU, April 2016 (2016-04-Q4-021), recommended for BBF TR-285



**“Dual slope” effect in EL-FEXT is now well understood**

**TNO**